

$$\begin{aligned} [2][a] \overrightarrow{QR} &= \langle 5-5, 5-1, -12-6 \rangle = \langle 10, 4, -6 \rangle \\ &= \boxed{10\vec{i} + 4\vec{j} - 6\vec{k}} \quad \textcircled{2} \end{aligned}$$

$$[b] \quad \vec{QP} = -\vec{PQ} = \langle -2, 3, 5 \rangle$$

$$2\vec{QP} - 3\vec{QR} = 2\langle -2, 3, 5 \rangle - 3\langle 10, 4, -6 \rangle$$

$$= \langle -4, 6, 10 \rangle - \langle 30, 12, -18 \rangle \textcircled{1}$$

$$= \langle -34, -6, 28 \rangle \textcircled{\frac{1}{2}}$$

$$[c] \|\vec{QR}\| = \sqrt{10^2 + 4^2 + (-6)^2} \quad \textcircled{\frac{1}{2}}$$

$$= 2\sqrt{5^2 + 2^2 + (-3)^2}$$

$$= 2\sqrt{25+4+9}$$

$$= \boxed{2\sqrt{38}} \quad \textcircled{\frac{1}{2}}$$

$$\textcircled{1} \left[-\frac{1}{2\sqrt{38}} \langle 10, 4, -6 \rangle \right] = \left\langle -\frac{5}{\sqrt{38}}, -\frac{2}{\sqrt{38}}, \frac{3}{\sqrt{38}} \right\rangle$$

$$= \left\langle \frac{-5\sqrt{38}}{38}, -\frac{\sqrt{38}}{19}, \frac{3\sqrt{38}}{38} \right\rangle \quad \textcircled{\frac{1}{2}}$$

$$[d] \quad \vec{QP} \times \vec{QS} = \begin{vmatrix} \vec{i} & \vec{j} & \vec{k} \\ -2 & 3 & 5 \\ -3 & 0 & 4 \end{vmatrix} \begin{vmatrix} \vec{i} & \vec{j} \\ -2 & 3 \\ -3 & 0 \end{vmatrix} = 12\vec{i} - 15\vec{j} + 8\vec{j} + 9\vec{k}$$

$$\left(\frac{1}{2}\right) \left[\langle 12, -7, 9 \rangle \right] \left(\frac{1}{2}\right)$$

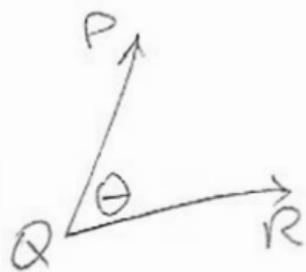
$$\langle 12, -7, 9 \rangle \cdot \langle -2, 3, 5 \rangle = -24 - 21 + 45 = 0$$

$$\langle 12, -7, 9 \rangle \cdot \langle -3, 0, 4 \rangle = -36 + 0 + 36 = 0$$

$$\left[\begin{array}{l} p \\ q \end{array} \right] \quad \frac{x+5}{3} = \frac{z+6}{4}, \quad y = 1 \quad \rightarrow \quad \frac{-x-5}{3} = \frac{z+6}{4}, \quad y = 1$$

1990 2000 2010 2020

$$[g] \quad \Theta = \cos^{-1} \frac{\vec{QP} \cdot \vec{QR}}{\|\vec{QP}\| \|\vec{QR}\|} = \cos^{-1} \frac{\langle -2, 3, 5 \rangle \cdot \langle 10, 4, -6 \rangle}{(\sqrt{(-2)^2 + 3^2 + 5^2}) (2\sqrt{38})}$$



$$= \cos^{-1} \frac{-20 + 12 - 30}{(\sqrt{38})(2\sqrt{38})}$$

$$= \cos^{-1} \frac{-38}{2 \cdot 38}$$

$$= \cos^{-1} -\frac{1}{2} = \frac{2\pi}{3} \text{ or } 120^\circ$$

SUBTRACT $\left(\frac{1}{2}\right)$ POINT
IF MISSING

[h]

	0	$\frac{1}{2}$	$\frac{1}{2}$
$x =$	-5	$+10t$	
$y =$	1	$+4t$	
$z =$	-6	$-6t$	

[3] [a] $\vec{w} \times \vec{u} = -(\vec{u} \times \vec{w}) = \boxed{-6\vec{i} - 3\vec{j}}$ or $\langle -6, -3, 0 \rangle$ ①

[b] $\vec{w} \times \vec{w} = \boxed{\vec{0}}$ ① (TRUE FOR ALL VECTORS) MUST HAVE ARROWHEAD (NO POINTS WITHOUT ARROWHEAD)

[c] $(\vec{v} \times \vec{w}) \cdot \vec{v} = \boxed{0}$ ① (CROSS PRODUCT OF 2 VECTORS IS ALWAYS PERPENDICULAR TO BOTH VECTORS)

$$[4] \vec{n} = \langle 0, 3, -1 \rangle \times \langle -3, 0, 2 \rangle = \begin{vmatrix} \vec{i} & \vec{j} & \vec{k} \\ 0 & 3 & -1 \\ -3 & 0 & 2 \end{vmatrix} \begin{matrix} \vec{i} \\ \vec{j} \\ \vec{k}} \end{matrix} = \boxed{6\vec{i} + 3\vec{j} + 9\vec{k}}$$

$\frac{1}{2}$
 $\frac{1}{2}$
 $\frac{1}{2}$

$$\langle 6, 3, 9 \rangle \cdot \langle 0, 3, -1 \rangle = \boxed{0 + 9 - 9 = 0}$$

$$\langle 6, 3, 9 \rangle \cdot \langle -3, 0, 2 \rangle = \boxed{-18 + 0 + 18 = 0}$$

$\frac{1}{2}$

$$2(x-0) + 1(y+3) + 3(z-2) = 0$$

$$\textcircled{1} \boxed{2x + (y+3) + 3(z-2) = 0} \quad \frac{1}{2}$$

↓

$$\text{USE } \vec{n} = \frac{1}{3} \langle 6, 3, 9 \rangle = \langle 2, 1, 3 \rangle$$